Expectations in the Cross Section:

# Stock Price Reaction to the Information in Bias and Analyst-Expected Returns 

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The Paper in a Nutshell...

$$
\begin{aligned}
\bar{R}_{t}^{A}= & \mathbb{E}\left[R_{t+1} \mid \mathcal{F}_{t}^{M}\right] \\
& +\mathbb{E}\left[R_{t+1} \mid \mathcal{F}_{t}^{A}\right]-\mathbb{E}\left[R_{t+1} \mid F_{t}^{M}\right] \\
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- The market-based expected return can be inferred by the investor
- The analyst's information component captures the (potential) improvement in estimating expected returns due to her superior information
- The analyst's bias captures how her reporting deviates from the rational expectation giving her information set
- The investors should update his expectation once $\bar{R}_{t}^{A}$ is reported. However, he should only react to the information component, not to the bias


## Estimating the Bias

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- Note that the investor can only observe the spread $S_{t}=\bar{R}_{t}^{A}-\mathbb{E}_{t}\left[R_{t+1} \mid F_{t}^{M}\right]$
not the information or the bias separately (depend on $\mathcal{F}_{t}^{A}$ )


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- Projecting the spread onto $\mathcal{F}_{t}^{M}$ yields

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S_{t}=\mathbb{E}\left[S_{t} \mid \mathcal{F}_{t}^{M}\right]+\epsilon_{\mathrm{t}}=\mathbb{E}\left[\operatorname{Bias} \mid \mathcal{F}_{t}^{M}\right]+\epsilon_{\mathrm{t}}
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- So, the investor has an estimate for the bias, $b_{t}=\mathbb{E}\left[\operatorname{Bias} \mid \mathcal{F}_{t}^{M}\right]$
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## Bayesian Updating of Expected Returns

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- A Bayesian investor would update:

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\mathbb{E}\left[R_{t+1} \mid \mathcal{F}_{t}^{M}, \bar{R}_{t}^{A}\right]=(1-\theta) \cdot \mathbb{E}\left[R_{t+1} \mid \mathcal{F}_{t}^{M}\right]+\theta \cdot\left(\bar{R}_{t}^{A}-b_{t}\right)
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1. If the investor is not Bayesian, then he update as:

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\mathbb{E}\left[R_{t, t+n}-R_{t, t} \mid \mathcal{F}_{t}^{M}, \bar{R}_{t}^{A}\right]=\left(\delta_{n}-\delta_{0}\right) \cdot i_{t}+\left(\gamma_{n}-\gamma_{0}\right) \cdot b_{t}
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$$

## Main Result

$$
\begin{gathered}
\mathbb{E}\left[R_{t, t+n} \mid \mathcal{F}_{t}^{M}, \bar{R}_{t}^{A}\right]=\delta_{n} \cdot i_{t}+\gamma_{n} \cdot b_{t} \\
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$$




## Outline

## The Paper

Comments

Final Remarks

## Assumptions 2 and 3

- Assumptions 2 and 3 effectively imply $\mathbb{E}\left[R_{t, t+n} \mid \mathcal{F}_{t}^{M}\right]=0$ and that is why you do not need to control for $\mathbb{E}\left[R_{t, t+n} \mid \mathcal{F}_{t}^{M}\right]$ in:

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$$

- Inconsistent methodology: uses $\mathbb{E}\left[R_{t+1} \mid \mathcal{F}_{t}^{M}\right]$ to get $b_{t}$, but then assumes $\mathbb{E}\left[R_{t, t+n} \mid \mathcal{F}_{t}^{M}\right]=0$ for the test


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- Correlation between $\mathbb{E}\left[R_{t+1} \mid \mathcal{F}_{t}^{M}\right]$ and $i_{t}$ or $b_{t}$ is a problem


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- Correlation between $\mathbb{E}\left[R_{t+1} \mid F_{t}^{M}\right]$ and $i_{t}$ or $b_{t}$ is a problem
- In the simple (no discount) model:

$$
\mathbb{E}\left[R_{t, t+n} \mid \mathcal{F}_{t}^{M}, \bar{R}_{t}^{A}\right]-\mathbb{E}\left[R_{t, t+n} \mid \mathcal{F}_{t}^{M}\right]=\delta_{n} \cdot i_{t}+\gamma_{n} \cdot b_{t}
$$

$$
\mathbb{E}\left[R_{t, t+n}-R_{t, t} \mid \mathcal{F}_{t}^{M}, \bar{R}_{t}^{A}\right]-\mathbb{E}\left[R_{t, t+n}-R_{t, t} \mid \mathcal{F}_{t}^{M}\right]=\left(\delta_{n}-\delta_{0}\right) \cdot i_{t}+\left(\gamma_{n}-\gamma_{0}\right) \cdot b_{t}
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\mathbb{E}\left[R_{t, t+n}-R_{t, t} \mid \mathcal{F}_{t}^{M}, \bar{R}_{t}^{A}\right]=\left(\delta_{n}-\delta_{0}\right) \cdot i_{t}+\left(\gamma_{n}-\gamma_{0}\right) \cdot b_{t}
\end{gathered}
$$

- Inconsistent methodology: uses $\mathbb{E}\left[R_{t+1} \mid \mathcal{F}_{t}^{M}\right]$ to get $b_{t}$, but then assumes $\mathbb{E}\left[R_{t, t+n} \mid \mathcal{F}_{t}^{M}\right]=0$ for the test
- Correlation between $\mathbb{E}\left[R_{t+1} \mid F_{t}^{M}\right]$ and $i_{t}$ or $b_{t}$ is a problem
- In the simple (no discount) model:

$$
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- Use this test (with your $\mathbb{E}\left[R_{t+1} \mid \mathcal{F}_{t}^{M}\right]$, not from Kelly et al)


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- You should at least provide robustness in which $\mathbb{E}\left[R_{t+1} \mid \mathcal{F}_{t}^{M}\right]-\mathbb{E}\left[R_{t+1} \mid \mathcal{F}_{t-1}^{M}\right]$ is controlled for in the regressions


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- My prior is that there is still bias. If I am wrong, this is a separate contribution as you will demonstrate how to extract the bias of analysts expected returns in a model-free manner


## Other Comments...

- Double sorted portfolios to control for $\mathbb{E}\left[R_{t+1} \mid \mathcal{F}_{t}^{M}\right]$ and $\mathbb{E}\left[R_{t+1} \mid \mathcal{F}_{t}^{M}\right]-\mathbb{E}\left[R_{t+1} \mid \mathcal{F}_{t-1}^{M}\right]$


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- Can you use the $b_{t}$ and $i_{t}$ to explain other short-lived anomalies?


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- Good luck!

