

Time-varying State Variable Risk Premia in the ICAPM

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$$M_{t+1} = \frac{\partial_W V(W_{t+1, z_{t+1}})}{\partial_W V(W_{t, z_t})}$$

- "The ICAPM simplify matters by assuming pure (retired) investors who sit on a pile of wealth, all invested in stocks and bonds....For this reason, the only state variables in the ICAPM are those that forecast future market returns" (Cochrane (2005), Ch. 9)
- Two possible approaches (assuming $\mathbb{E}_t[R_w] = \boldsymbol{b} \times z_t$):

 $M_{t+1} = \frac{\partial_{W} V(W_{t+1}, z_{t+1})}{\partial_{W} V(W_{t}, z_{t})}$ $\approx a_{t} + W_{t} \frac{\partial_{WW} V_{t}}{\partial_{W} V_{t}} \times \frac{\Delta W_{t+1}}{W_{t}} + \frac{\partial_{Wz} V_{t}}{\partial_{W} V_{t}} \times \Delta z_{t+1}$

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$$= a_t - \gamma_t \times R_{w,t+1} - \phi_t \times \Delta z_{t+1}$$

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The Paper

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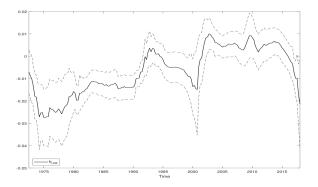


Figure 1: Rolling coefficients of consumption growth on lagged risk-free rate

This figure presents coefficient estimates, $b_{l,RF}$, from a rolling ten-year regression of quarterly consumption growth on the lagged three month t-bill rate (±1.65 Newey and West, 1987, standard error bands).

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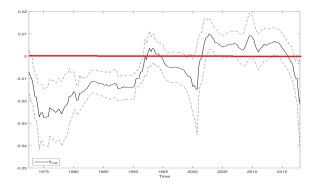


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6.37

3.02

4.78

3.37

 $R^{2}(\times 100)$

 $R_{t+1} = \beta_t \cdot \lambda_{t+1}$ with $\mathbb{E}[\lambda_{t+1}] = \phi_t \times \sigma_{z,t}^2$

Fixed effects		\checkmark
g_0	$0.00 \\ (0.00)$	
b_{t,z_k}	$270.68 \\ (1.95)$	$252.42 \\ (1.91)$
σ_{t,z_k}^2	$\begin{array}{c} 0.56 \\ (0.54) \end{array}$	$0.56 \\ (0.58)$
$b_{t,z_k} imes \sigma_{t,z_k}^2$	$185.86 \\ (1.95)$	185.91 (2.00)
$R^{2}(\times 100)$	5.00	6.75

The Paper

$R_{t+1} = \beta_t \cdot \lambda_{t+1}$ with	$\mathbb{E}[\lambda_{t+1}]$	$] = \phi_t \times \sigma_{z,t}^2$
Fixed effects		\checkmark
Low b_{t,z_k} , High σ_{t,z_k}^2	-4.36 (-2.64) [-2.36]	-4.19 (-2.42) [-2.11]
Low b_{t,z_k} , Low σ_{t,z_k}^2	-2.90 (-2.13) [-2.14]	-2.73 (-1.96) [-1.77]
High b_{t,z_k} , Low σ_{t,z_k}^2	$2.44 \\ (1.62) \\ [1.69]$	2.27 (1.67) [1.42]
High b_{t,z_k} , High σ_{t,z_k}^2	$ \begin{array}{r} 4.73 \\ (1.93) \\ [2.28] \end{array} $	$\begin{array}{c} 4.56 \\ (2.12) \\ [2.05] \end{array}$
HH - LH	$9.09 \\ (2.86) \\ [2.85]$	8.74 (3.01) [2.47]

Outline

The Paper

Comments

Final Remarks

- "...the only state variables in the ICAPM are those that forecast future market returns" (Cochrane (2005), Ch. 9)
- This paper: "As argued by Roll (1977), the aggregate stock market return can be a poor proxy for the return on aggregate wealth...we follow the advice in Cochrane (2005, Ch. 9) and seek instead recession state variables"
- The argument goes against using R_w in the SDF
- "...expected returns may depend on additional betas that capture labor market conditions, house values, fortunes of small business, or other non-marketed assets. Yet these state variables need not forecast returns on any traded assets--this is not the ICAPM. Much current empirical work seems to be headed towards additional state variables of this type for distress, recession, etc..."
- Treat Δc as a feature, not a bug!

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Comment 2: ϕ_t allows for more than Campbell (1993)

• With Epstein-Zin preferences (see Campbell (1993)):

 $log(M_{t+1}) = \gamma \times r_{w} + (\gamma - 1) \times \Delta \mathbb{E}_{t} [\sum_{h=1}^{h=\infty} \rho^{h} \cdot r_{w,t+h}]$ $= \gamma \times r_{w} + (\gamma - 1) \cdot \rho \cdot B \cdot (1 - \rho \cdot B)^{-1} \times \Delta \rho$

- In some sense, Campbell (1993)'s framework provides a much stricter test of the ICAPM than Cor(φ, b)>0
- Why should we care about the weaker test then?
- Because the test allows for time-varying predictability, which is empirically important
- **B**_t in Campbell (1993)'s framework is not tractable
- This is a clear contribution of this paper...but never discussed

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- 2. Does the behavior of γ make sense?
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R^2 from $b_t = d_0 + d_1 \times z_t + \epsilon_t$					
Model 1		Model 2			
DY	DS	TS	DY	DS	RF
15%	10%	67%	16%	32%	65%
Model 3			Model 4		
PE	VS	TS	DY	СР	LVL
8%	41%	57%	34%	33%	54%

Comment 4: Risk Premia on Standard "Risk Factors"

$$HML_{t+1} = a + \beta_m \times (R_{m,t+1} - R_{f,t+1}) + \beta_\lambda \times \lambda_{t+1}$$

 $\mathbb{E}_t[HML_{t+1}] = a + \beta_m \times \overline{R_m - R_f} + \beta_\lambda \times \mathbb{E}_t[\lambda_{t+1}]$

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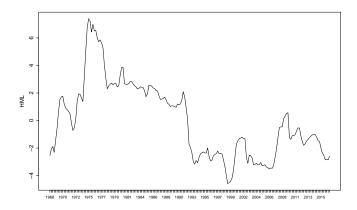
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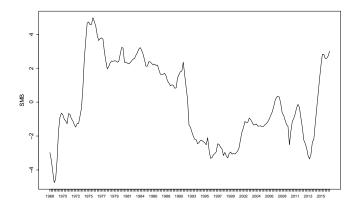
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- Why 4 models? I would merge them into one model with 6 state variables
- 2. Orthogonalizing z relative to R_w breaks the link between model and empirical implementation, making the economic interpretation difficult
- Instead of assuming zs are orthogonal, why not using univariate βs so that E[λ_{t+1}] = φ_t × σ²_{z,t} is valid regardless of the correlation structure in z (see Cochrane (2005) Ch. 13.4)
- 4. "...the ICAPM of Merton (1973) can be collapsed to the consumption CAPM under the restrictive assumption of time-separable preferences...Thus. our estimates will speak to what preference structure is needed to fully explain conditional state variable risk premia."

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- 4. "...the ICAPM of Merton (1973) can be collapsed to the consumption CAPM under the restrictive assumption of time-separable preferences...Thus. our estimates will speak to what preference structure is needed to fully explain conditional state variable risk premia."

Outline

The Paper

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