

Fundamental Anomalies

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Outline

The Paper

My Comments

• Firm's Net Present Value (NPV) Rule:

q-theory formalizes this logic and implies: $|R^S = R^I$

• Firm's Net Present Value (NPV) Rule:

 $NPV = Inv \partial Benefit - Inv \partial Cost$ $= \widehat{CF}(I)/(1 + WACC) - Cost(I)$ $0 = \mathbb{E}[CF(I^*)]/\mathbb{E}[R] - Cost(I^*)$ \downarrow $E[R] = \mathbb{E}[CF(I^*)]/Cost(I^*)$

q-theory formalizes this logic and implies: $|R^S|$

• Firm's Net Present Value (NPV) Rule:

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 - $0 = \mathbb{E}\left[CF\left(I^*\right)\right]/\mathbb{E}\left[R\right] Cost\left(I^*\right)$

 $\mathbb{E}\left[R\right] = \mathbb{E}\left[CF\left(l^*\right)\right] / Cost\left(l^*\right)$

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q-theory formalizes this logic and implies: $R^{S} = R^{k}$

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$\mathbb{E}\left[R\right]$ from Firm's Perspective

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The Empirical Challenge of $\mathbb{E}[R^S] = \mathbb{E}[R^F]$

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Campbell (2017): The Empirical Challenge Matters



"This problem, that different parameters are needed to fit each anomaly, is a pervasive one in the q-theoretic asset pricing literature (p. 275)."

Gonçalves, Xue, and Zhang (2020, RFS)

$$r_{p}^{F} = r^{F} \left(r_{p}^{Ba}; w_{p}^{B}; \frac{I_{p}}{K_{p}}; \frac{Y_{p}}{K_{p}}; \delta_{p} \right)$$

$$r_p^F = \sum_{i=1}^{n_p} w_{ip} \times r^F \left(r_i^{Ba}; w_i^B; \frac{l_i}{K_i}; \frac{l_i}{K_i}; \frac{Y_i}{K_i + W_i}; \frac{K_i}{K_i + W_i}; \delta_i \right)$$

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Consumer Nondurables: γ

Consumer Nondurables: a



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Business Equipment: γ





Business Equipment: a



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$\mathbb{E}[r]$ for 12 Anomalies



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Aggregate Returns



Outline

The Paper

My Comments

$$r_{it+1}^{S} = r_{it+1}^{F} + \varpi_{it}^{-1/2} \cdot \sigma_{r} \cdot e_{it+1}^{r}$$
 with $e_{it}^{r} \stackrel{iid}{\sim} N(0,1)$

• $r_{it}^F = r^F(Data; \theta_{jt})$ and $\varpi_{it} = V_{it} / \sum_{i=1}^{N_{jt}} V_{it}$

- Paper explores the effect of *j* and *t*, but not of the Bayesian framework
- You can estimate θ_{jt} at each t and for each j (by NLS)
- How much does the fit improve as you change from the Frequentist (NLS) to the Bayesian (MCMC) framework?

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The Paper

1) Compare Bayesian and Frequentist Methods

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• (ii) Variation in *a_{jt}*

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 $\circ \Pi_{it} = \gamma \cdot Y_{it}$ (Gonçalves, Xue, and Zhang (2020))

 \circ Is variation in γ_{jt} in line with variation in Π_{jt}/Y_{jt} ?

• Gross profits (Sales - COGS) provides a rough estimate for Π_{jt}

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- (ii) Variation in a_{jt}
 - $(V_{it} + B_{it+1})/K_{it} = Q_{it} = (1 + a_{jt} \cdot (1 \tau_t) \cdot I_{it}/K_{it}) + W_{it}/K_{it}$
 - Is variation in a_{jt} in line with variation in Q_{jt} ?
 - Is variation in a_{jt} in line with the sensitivity of Q_{it} to I_{it}/K_{it} ?

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• Impossible to perfectly align r_{it}^{S} and r_{it}^{F}

- Not relevant for prior papers as they rely on (portfolio) $\mathbb{E}[r]$
- Very relevant for this paper
- Overfitting: time-varying θ_{jt} compensates for misalignment
- This is why the specification with $heta_j$ performs better OOS

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• (i) Autocorrelation "Solution"

• Misalignment generates autocorrelation in observed $r_{it}^S - r_{it}^F$ • $e_{it}^r \stackrel{iid}{\sim} N(0, 1)$ forces θ_{jt} to be artificially autocorrelated

- $\circ\,$ Solution: allow for autocorrelation in e^r_{it}
- (ii) Return Unsmoothing "Solution":

$$r_{it+1}^{S} = r_{it+1}^{F} + \varpi_{it}^{-1/2} \cdot \sigma_{r} \cdot e_{it+1}^{r} \qquad \text{with } e_{it}^{r} \stackrel{iid}{\sim} N(0,1)$$

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• Misalignment generates autocorrelation in observed $r_{it}^{S} - r_{it}^{F}$ • $e_{it}^{R} \stackrel{\text{def}}{\to} N(0, 1)$ forces θ_{it} to be artificially autocorrelated • Solution: allow for autocorrelation in e_{it}^{R}

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 - Couts, Gonçalves, and Rossi (2020)
 - Observed r_{it}^F is a Moving Average of true r_{it}^F
 - MA parameters assure $r_{it}^S r_{it}^F$ is uncorrelated
 - Recover r^F_{it} and use $r^S_{it+1} = r^F_{it} + \varpi^{-1/2}_{it} \cdot \sigma_r \cdot e^r_{it+1}$

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 - Observed r_{it}^F is a Moving Average of true r_{it}^F
 - MA parameters assure $r_{it}^{S} r_{it}^{F}$ is uncorrelated
 - Recover r_{it}^F and use $r_{it+1}^S = r_{it}^F + \varpi_{it}^{-1/2} \cdot \sigma_r \cdot e_{it+1}^r$

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• In section 5.5 (Equation 10), I suggest you also explore:

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- \circ In line with the data (e.g., FF data implies 4.8% decline)
- $\circ~$ But the r_t^S value premium declines by less than 1% in your data
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Outline

The Paper

My Comments

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- Strong response to the criticism that the investment model needs different parameter estimates for different anomalies
- Provides a methodological foundation for future work
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